L6: Reasoning logically - rule-based systems (Applications of Forward- and Backward-chaining algorithms)

- Review of inference mechanisms
- Rule-based system and its implementation in Java

Seven inference rules for propositional Logic

• R(1) Modus Ponens $\alpha \Rightarrow \beta, \alpha$ • R(2) And-Elimination $\alpha_1 \land \alpha_2 \land \ldots \land \alpha_n$ α_{i} • R(3) And-Introduction $\alpha_1, \alpha_2, ..., \alpha_n$ $\alpha_1 \wedge \alpha_2 \wedge \ldots \wedge \alpha_n$ α_i • R(4) Or-Introduction $\alpha_1 \vee \alpha_2 \vee \ldots \vee \alpha_n$ • R(5) Double-Negation Elimination $\neg \neg \alpha$ • R(6) Unit Resolution $\frac{\alpha \lor \beta, \neg \beta}{\alpha}$ • R(7) Logic connectives: $\frac{\alpha \lor \beta, \neg \beta \lor \gamma}{\alpha \lor \gamma}$

The three new inference rules

Ground term is a

term that contains

no variables.

α

 $\exists v \text{ SUBST}(\{g/v\}, \alpha)$

• R (8) Universal Elimination: For any sentence α , variable *v*, and ground term g:

 $\forall v \alpha$

SUBST($\{v/g\}, \alpha$)

e. g., $\forall x \ Likes(x, IceCream)$, we can use the substitute {*x/Rose*} and infer *Like(Rose, IceCream*).

• R (9) Existential Elimination: For any sentence α , variable ν , and constant **x**

k that does not appear elsewhere in the knowledge base:

 $\exists v \alpha$

SUBST($\{v/k\}, \alpha$)

e. g., $\exists x \; Kill(y, Victim)$, we can infer *Kill(Murderer, Victim)*, as long as *Murderer* does not appear elsewhere in the knowledge base.

 R (10) Existential Introduction: For any sentence α, variable *v* that does not occur in α, and ground term g that does occur in α:

e. g., from *Likes(Rose, IceCream)*

we can infer $\exists x \ Likes(x, IceCream)$.



Example of proof (証明)

Bob is a buffalo	1. Buffalo(Bob)	fl
Pat is a pig	2. <i>Pig(Pat)</i>	- <i>f</i> 2
Buffaloes run faster than pigs	$ 3. \forall x, y Buffalo(x) \land Pig(y) \Rightarrow Faster(x,y)$	-r1
To proof:		
10 proof.		
Bob runs faster than P	at	
Apply R(3) to <i>f1</i> And <i>f</i> 2	4. Buffalo(Bob) ∧ Pig(Pat)	f3
		v
(And-Introduction)		
Apply R(8) to <i>r1</i> {x/Bob, y/Pat	$ 5. Buffalo(Bob) \land Pig(Pat) \Rightarrow Faster(Bob, Pat) $	at)f4
(Universal-Elimination)		
Apply $R(1)$ to $f3$ And $f4$	6 . <i>Faster(Bob,Pat)</i>	f5
(Inplication-Elimination)		

Search with primitive (基本の) inference rules

Operators are inference rules

States are sets of sentences

Goal test checks state to see if it contains query (質問) sentence



R(1) to R(10) are common inference pattern

Problem: branching factors are huge, esp. for R(8)

Idea: find a substitution that makes the rule premise

match some known facts.

Stored in working memory Stored in rule base



Unify

Unification function substitution that wou	, <mark>Unify</mark> , is to take two atom ald make <i>p</i> and <i>q</i> look the s	nic sentences p and q and return a same.
A substitute λ unifie	s atomic sentences p and q	if $p \lambda = q \lambda$
For example,		
р	q	λ
Knows(John, x)	Knows(John, Jane)	{x/Jane}
Knows(John, x)	Knows(y, OJ)	{y/John, x/OJ}
Knows(John, x)	Knows(y, Mother(y))	{y/John, x/Mother(John)}
 nise 前提		





```
public boolean matching(String string1, String string2) {
        // System.out.println(string1);
        // System.out.println(string2);
        // 同じなら成功
        if (stringl.equals(string2))
                return true;
        // 各々トークンに分ける
        st1 = new StringTokenizer(string1);
        st2 = new StringTokenizer(string2);
        // 数が異なったら失敗
        if (st1.countTokens() != st2.countTokens())
                return false:
        // 定数同士
        for (int i = 0; i < st1.countTokens();) {</pre>
                if (!tokenMatching(st1.nextToken(), st2.nextToken())) {
// トークンが一つでもマッチングに失敗したら失敗
                        return false;
        }
        // 最後まで 0.K. なら成功
        return true:
 boolean tokenMatching(String token1, String token2) {
         // System.out.println(token1+"<->"+token2);
         if (token1.equals(token2))
                 return true;
         if (var(token1) && !var(token2))
                 return varMatching(token1, token2);
         if (!var(token1) && var(token2))
                 return varMatching(token2, token1);
         return false:
```



Forward chaining

If we start with the sentences in the knowledge base and generate new conclusions that in turn can allow more inferences to be made. This is called forward chaining.

when a new fact p is added (told) to the KB

for each rule such that *p* unifies with a premise

if the other premises are known

then add the conclusion to the KB and continue chaining.

- 新しい事実が観測されたときに、事実に最も合う推論を求める
 事実からスタートして、ルールによって推論結果を得る
 新たに得られた推論結果は、東京と同じとうに次の推論に利用でき
- ・新たに得られた推論結果は、事実と同じように次の推論に利用できる
- ・「AはBである」という事実と、「BならばC」という規則から、「AはCである」と いう結論を導く推論方式
- Forward chaining is usually used when a new fact is added to the database and we want to generate its consequences.

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• It is data driven.

Forward chaining example

Let us add facts r1, r2, r3, f1, f2, f3 in turn into KB.

 $r1. Buffalo(x) \land Pig(y) \Rightarrow Faster(x,y)$ $r2. Pig(y) \land Slug(z) \Rightarrow Faster(y,z)$ $r3. Faster(x,y) \land Faster(y,z) \Rightarrow Faster(x,z)$ f1. Buffalo(Bob)[r1-c1, Bob/x, yes]f2. Pig(Pat)[r1-c2, Pat/y, yes]f4. Faster(Bob, Pat)f3. Slug(Steve)[r2-c2, Steve/z, yes][r2, f2, f3, Pat/y, Steve/z, yes] $r3, f4, f5, Bob/x, Pat/y, Steve/z, yes] \rightarrow f6. Faster(Bob, Steve)$



Rules defined in the rule base file: CarShop

rule "CarRule1" "?x is inexpensive" if then "?x is made in Japan" rule "CarRule2" "?x is small" if then "?x is made in Japan" rule "CarRule3" "?x is expensive" if then "?x is a foreign car" rule "CarRule4" if "?x is big" "?x needs a lot of gas" then "?x is a foreign car" rule "CarRule5" if "?x is made in Japan" "?x has Toyota's logo" then "?x is a Toyota" rule "CarRule6" if "?x is made in Japan" "?x is a popular car" then "?x is a Toyota"

rule "CarRule7" "?x is made in Japan" if "?x has Honda's logo" then "?x is a Honda" rule "CarRule8" "?x is made in Japan" if "?x has a VTEC engine" then "?x is a Honda" rule "CarRule9" "?x is a Toyota" if "?x has several seats" "?x is a wagon" then "?x is a Carolla Wagon" rule "CarRule10" if "?x is a Toyota" "?x has several seats" "?x is a hybrid car" then "?x is a Prius" rule "CarRule11" if "?x is a Honda" "?x is stylish" "?x has several color models" "?x has several seats" "?x is a wagon" then "?x is an Accord Wagon"

rule "CarRule12" "?x is a Honda" if "?x has an aluminium body" "?x has only 2 seats" then "?x is a NSX" rule "CarRule13" "?x is a foreign car" if "?x is a sports car" "?x is stylish" "?x has several color models" "?x has a big engine" then "?x is a Lamborghini Countach" rule "CarRule14" "?x is a foreign car" if "?x is a sports car" "?x is red" "?x has a big engine" then "?x is a Ferrari F50" rule "CarRule15" "?x is a foreign car" if "?x is a good face" then "?x is a Jaguar XJ8"

Forward Chaining.他の例



<u>rules</u>



Backward chaining

It is to start with something we want to prove, find implication sentences that would allow us to conclude it, and them attempt to establish their premises in turn. This <u>is called backward chaining</u>.

when a query q is asked

if a matching fact q' is known, return the unifier

for each rule whose consequent q' match q

ASK

attempt to prove each premise of the rule by backward chaining

・与えられた仮説が、現在のアサーション集合において成り立つかどうかを検証していく推論
 ・ゴールからスタートする、ゴールが事実の集合にあれば推論成功



Backward chaining example



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Rules defined in the rule base file: CarShop

rule "CarRule1" "?x is inexpensive" if then "?x is made in Japan" rule "CarRule2" "?x is small" if then "?x is made in Japan" rule "CarRule3" "?x is expensive" if then "?x is a foreign car" rule "CarRule4" if "?x is big" "?x needs a lot of gas" then "?x is a foreign car" rule "CarRule5" if "?x is made in Japan" "?x has Toyota's logo" then "?x is a Toyota" rule "CarRule6" if "?x is made in Japan" "?x is a popular car" then "?x is a Toyota"

rule "CarRule7" "?x is made in Japan" if "?x has Honda's logo" then "?x is a Honda" rule "CarRule8" "?x is made in Japan" if "?x has a VTEC engine" then "?x is a Honda" rule "CarRule9" "?x is a Toyota" if "?x has several seats" "?x is a wagon" then "?x is a Carolla Wagon" rule "CarRule10" if "?x is a Toyota" "?x has several seats" "?x is a hybrid car" then "?x is a Prius" rule "CarRule11" if "?x is a Honda" "?x is stylish" "?x has several color models" "?x has several seats" "?x is a wagon" then "?x is an Accord Wagon"

rule "CarRule12" "?x is a Honda" if "?x has an aluminium body" "?x has only 2 seats" then "?x is a NSX" rule "CarRule13" "?x is a foreign car" if "?x is a sports car" "?x is stylish" "?x has several color models" "?x has a big engine" then "?x is a Lamborghini Countach" rule "CarRule14" "?x is a foreign car" if "?x is a sports car" "?x is red" "?x has a big engine" then "?x is a Ferrari F50" rule "CarRule15" "?x is a foreign car" if "?x is a good face" then "?x is a Jaguar XJ8"

Backward Chaining.他の例



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Rule-base System Examples



loadRules method

```
private void loadRules(String theFileName) {
        String line;
        trv {
                int token;
                f = new FileReader("src/tes/" + theFileName);
                st = new StreamTokenizer(f);
                while ((token = st.nextToken()) != StreamTokenizer.TT_EOF) {
                        switch (token) {
                        case StreamTokenizer.TT_WORD:
                                 String name = null;
                                 ArrayList<String> antecedents = null;
                                 String consequent = null;
                                 if ("rule".equals(st.sval)) {
                                         if (st.nextToken() == '"') {
                                                 name = st.sval;
                                                 st.nextToken();
                                                 if ("if".equals(st.sval)) {
                                                         antecedents = new ArrayList<String>();
                                                         st.nextToken();
                                                         while (!"then".equals(st.sval)) {
                                                                  antecedents.add(st.sval);
                                                                  st.nextToken();
                                                         if ("then".equals(st.sval)) {
                                                                  st.nextToken():
                                                                  consequent = st.sval;
                                                 }
                                         ļ
                                 rules.add(new Rule(name, antecedents, consequent));
                                 break:
                        default:
                                 System.out.println(token):
                                 break;
        } catch (Exception e) {
                System.out.println(e):
```

Rule-base System Examples (1)

public class RuleBaseSystem {
 static RuleBase rb;
 public static void main(String args[]){
 rb = new RuleBase();
 rb.forwardChain();
 }
}



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```
public void forwardChain() {
      boolean newAssertionCreated;
      // 新しいアサーションが生成されなくなるまで続ける.
      do {
             // 新しいアサーションが生成されたかどうかを保存する変数
             newAssertionCreated = false;
             // ルールの数だけルーブ
             Rule aRule = rules.get(i);
                    // 取り出されたルールの表示
                    System.out.println("apply rule:" + aRule.getName());
                    // ルールの前件を表示
                    ArrayList<String> antecedents = aRule.getAntecedents();
                    // ルールの後件を表示
                    String consequent = aRule.getConsequent();
                    // バインディング情報の取得
                    ArrayList<HashMap<String, String>> bindings = wm
                                  .matchingAssertions(antecedents);
                    if (bindings != null) {
                           for (int j = 0; j < bindings.size(); j++)</pre>
                                  // 後件をインスタンシエーション(変数にバインディング情報を当てはめる)
                                 String newAssertion = instantiate((String) consequent,
                                               bindings.get(j));
                                  // ワーキングメモリーになければ成功
                                  if (!wm.contains(newAssertion)) {
                                        System.out.println("Success: " + newAssertion);
                                        // 持っている知識に追加
                                        wm.addAssertion(newAssertion);
                                        newAssertionCreated = true:
             System.out.println("Working Memory" + wm);
       } while (newAssertionCreated);
      System.out.println("No rule produces a new assertion");
```

matchable() Method

```
public ArrayList<HashMap<String, String>> matchingAssertions(
               ArravList<String> theAntecedents) {
       ArrayList<HashMap<String, String>> bindings = new ArrayList<HashMap<String, String>>();
        return matchable(theAntecedents, 0, bindings);
}
 private ArrayList<HashMap<String, String>> matchable(
                ArrayList<String> theAntecedents, int n,
                ArrayList<HashMap<String, String>> bindings) {
         // 前件の数だけ繰り返す
         if (n == theAntecedents.size()) {
                return bindings;
         // 1つ目
         else if (n == 0) {
                boolean success = false;
                // わかっている知識の数だけループ
                for (int i = 0; i < assertions.size(); i++) {
// バインディング情報を保持するハッシュマップ
                        HashMap<String, String> binding = new HashMap<String, String>();
                        // マッチングに成功
                        if ((new Matcher()).matching(theAntecedents.get(n),
                                        assertions.get(i), binding)) {
                                // バインディング情報をハッシュマップに追加
                                bindings.add(binding):
                                success = true;
                if (success) {
                        return matchable(theAntecedents, n + 1, bindings):
                } else {
                        return null;
         }
```

```
// 2つ目以降
else {
         boolean success = false;
        // バインディング情報を保持するハッシュマップ
         ArrayList<HashMap<String, String>> newBindings = new ArrayList<HashMap<String, String>>();
        // 得られたバインディング情報の数だけループ
        for (int i = 0; i < bindings.size(); i++) {
// わかっている知識の数だけループ
                 for (int j = 0; j < assertions.size(); j++) {</pre>
                          // マッチングに成功
if ((new Matcher()).matching(theAntecedents.get(n),
                                  assertions.get(j), bindings.get(i))) {
// バインディング情報をハッシュマップに追加
newBindings.add(bindings.get(i));
                                   success = true;
         if (success) {
                 return matchable(theAntecedents, n + 1, newBindings);
         } else {
                 return null;
}
```

前向き推論の解説

はじめに

ソース内に出てくる変数名に使われている単語 は以下の意味がある

- Assertion :わかっている知識(my-car is a wagon等)
- Antecedents:前件(ルールの条件,IFの部分)
- Consequent:後件(ルールから得られる結論, THENの部分)
- Bindings : 法合(知識と前件・後件の変数を結びつける)

前向き推論の途中まで

public void forwardChain() { boolean newAssertionCreated; // 新しいアサーションが生成されなくなるまで続ける. CarRule1 do { // 新しいアサーションが生成されたかどうかを保存する変数 newAssertionCreated = false; // ルールの数だけループ "?x is inexpensive" for (int i = 0; i < rules.size(); i++) { // ルールを取り出す Rule aRule = rules.get(i); // 取り出されたルールの表示 System.out.println("apply rule:" + aRule.getName()); // ルールの前件を取得 "?x is made in Japan" ArrayList<String> antecedents = aRule.getAntecedents(); // ルールの後件を取得 String consequent = aRule.getConsequent(); ?x=my-car // バインディング情報の取得 ArrayList<HashMap<String, String>> bindings = wm .matchingAssertions(antecedents);

前向き推論の続き

my-car is made in Japan

```
if (bindings != null) {
          for (int j = 0; j < bindings.size(); j++) {
                    // 後件をインスタンシエーション(変数にバインディング情報を当てはめる)
                    String newAssertion = instantiate((String) consequent, bindings.get(j));
                    // ワーキングメモリーになければ成功
                    if (!wm.contains(newAssertion)) {
                              System.out.println("Success: " + newAssertion);
                              // 持っている知識に追加
                              wm.addAssertion(newAssertion);
                              newAssertionCreated = true;
                                                               ワークングメモリーの中
                                                              my-car is inexpensive
System.out.println("Working Memory" + wm);
                                                              my-car has a VTEC engine
//全てのルールを見て1つでも知識が追加されたら、1から見直す
while (newAssertionCreated);
                                                              my-car is made in Japan
System.out.println("No rule produces a new assertion");
```

matchingAssertionsメソッド

引数は、そのルールの前件で、ルールに含まれる変数を知識 と結びつけたものを返す

public ArrayList<HashMap<String, String>> matchingAssertions(
ArrayList<String> theAntecedents) {

//変数と知識を結びつけた HashMapを保持するリスト
ArrayList<HashMap<String, String>> bindings = new
ArrayList<HashMap<String, String>>();
return matchable(theAntecedents, 0, bindings);

Matchableメソッド

```
// 前件の数だけ繰り返す
if (n == theAntecedents.size()) {
                                            ルールの前件の数だけ持っている知識と繰り返
           return bindings;
                                            してマッチングを行いバインディング情報を返す
}
// 1つ目
else if (n == 0) {
  boolean success = false;
  //わかっている知識の数だけループ
  for (int i = 0; i < assertions.size(); i++) {</pre>
           // バインディング情報を保持するハッシュマップ
           HashMap<String, String> binding = new HashMap<String, String>();
           //マッチングに成功
           if ((new Matcher()).matching(theAntecedents.get(n), assertions.get(i), binding)) {
                      // バインディング情報をハッシュマップに追加
                      bindings.add(binding);
                      success = true;
           }
  }
  if (success) {
           return matchable(theAntecedents, n + 1, bindings);
  } else {
           return null;
  }
```

1個目のマッチング

- Matcherクラスのmatchingメソッドで知識と前 件の照合を行い、バインディング情報を得る
- 例:CarRule8



Matchableメソッド

```
else {
  boolean success = false;
  // バインディング情報を保持するハッシュマップ
  ArrayList<HashMap<String, String>> newBindings = new ArrayList<HashMap<String, String>>();
  // 得られたバインディング情報の数だけループ
  for (int i = 0; i < bindings.size(); i++) {</pre>
           //わかっている知識の数だけループ
           for (int j = 0; j < assertions.size(); j++) {</pre>
                       //マッチングに成功
                       if ((new Matcher()).matching(theAntecedents.get(n),assertions.get(j), bindings.get(i))) {
                                   // バインディング情報をハッシュマップに追加
                                   newBindings.add(bindings.get(i));
                                   success = true;
                       }
                                                                前件が複数ある場合は、マッチン
           }
                                                                グに既知のバインディング情報に
  }
  if (success) {
                                                                追加する
           return matchable(theAntecedents, n + 1, newBindings);
  } else {
           return null;
```

2個目以降のマッチング

1個目の前件と知識の照合で得た?x=my-car
 というバインディング情報も利用してマッチング



rule	"CarRule1"	rule
if	"?x is inexpensive"	if
then	"?x is made in Japan"	
	-	then
Rule	"CarRule2"	
if	"?x is small"	rule
then	"?x is made in Japan"	if
rule	"CarRule3"	then
If	"?x is expensive"	
then	"?x is a foreign car"	rule
	6	if
rule	"CarRule4"	
if	"?x is big"	
	"?x needs a lot of gas"	then
then	"?x is a foreign car"	
	e	rule
Rule	"CarRule5"	if
If	"?x is made in Japan"	
"?x has	Toyota's logo"	
then	"?x is a Toyota"	then
rule	"CarRule6"	rule
if	"?x is made in Japan"	if
	"?x is a popular car"	
Then	"?x is a Toyota"	

rule if	"CarRule7" "?x is made in Japan"
	"?x has Honda's logo"
then	"?x is a Honda"
rule	"CarRule8"
if	"?x is made in Japan"
	"?x has a VTEC engine"
then	"?x is a Honda"
rule	"CarRule9"
if	"?x is a Toyota"
	"?x has several seats"
	"?x is a wagon"
then	"?x is a Carolla Wagon"
rule	"CarRule10"
if	"?x is a Toyota"
	"?x has several seats"
	"?x is a hybrid car"
then	"?x is a Prius"
rule	"CarRule11"
if	"?x is a Honda"
	"?x is stylish"
	"?x has several color models"
	"?x has several seats"

"?x is a wagon"

then

"?x is an Accord Wagon"

rule	"CarRule12"
if	"?x is a Honda"
	"?x has an aluminium body"
	"?x has only 2 seats"
then	"?x is a NSX"
rule	"CarRule13"
if	"?x is a foreign car"
	"?x is a sports car"
	"?x is stylish"
	"?x has several color models"
	"?x has a big engine"
then	"?x is a Lamborghini Countach"
rule	"CarRule14"
if	"?x is a foreign car"
	"?x is a sports car"
	"?x is red"
	"?x has a big engine"
then	"?x is a Ferrari F50"
rule	"CarRule15"
if	"?x is a foreign car"
	" ⁹ x is a good face"
then	"?x is a Jaguar XI8"

Facts in Working Memory (WM):

his-car is inexpensive his-car has a VTEC engine his-car is stylish his-car has several color models his-car has several seats his-car is a wagon



Output:





Forward Chaining



Exercise – AI programming

- 1. Input program <u>RuleBaseSystem.java</u>, and a rule-base file <u>CarShop.txt</u> understand them, run the program, and check the output.
- Make some modifications to RuleBaseSystem.java

 (data file name: Outruns.data, rules in the data file, and
 writing the initial content (facts) in the working memory in a file, wm.txt)
 so that the program can run for the following case.

Bob is a buffalo	1. Buffalo(Bob)	
Pat is a pig	2. <i>Pig(Pat)</i>	
Buffaloes outrun pigs	3. ∀ x, y Buffalo(x) ∧ $Pig(y) \Rightarrow Faster(x,y)$	
Bob outruns Pat		
Apply (3) to 1 And 2	$ 4. Buffalo(Bob) \land Pig(Pat)$	
Apply (8) to 3 {x/Bob, y/Pat} 5. <i>Buffalo(Bob)</i> \land <i>Pig(Pat)</i> \Rightarrow <i>Faster(Bob,Pat)</i>		
Apply (1) to 4 And 5	6. <i>Faster(Bob,Pat)</i>	

Output:

🔀 BootStrap RuleBaseSystem



```
AppAccelerator(tm) 1.2.010 for Java (JDK 1.2), x86 version.
Copyright (c) 1997-1999 Inprise Corporation. All Rights Reserved.
ADD:Buffalo(Bob)
ADD:Pig( Pat )
r3 [?X, ?Y]->?X & ?Y
apply_rule:r3
apply rule:f3
Success: Faster( Bob , Pat )
ADD:Faster( Bob , Pat )
Working Memory[Buffalo( Bob ), Pig( Pat ), Fast<u>er( Bob , Pat )]</u>
lapply rule:r3
lapply rule:f3
Working Memory[Buffalo( Bob ), Pig( Pat ), Faster( Bob , Pat )]
No rule produces a new assertion
```

アブリケーションを停止するには Ctrl+C を押してください

Home work

Write a report includes

- Front page (name, id)
- About the report
 - exercise problem statement
 - Where you make effort
- Source program
- Execution screen shot

The submission deadline: 2015/11/05